

SPHERE non-common path aberrations measurement and pre-compensation with optimized phase diversity processes

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ONERA

Outline

Specificities of SPHERE NCPA calibration

Baseline solution

- Presentation
- First experimental results on SAXO bench

safe

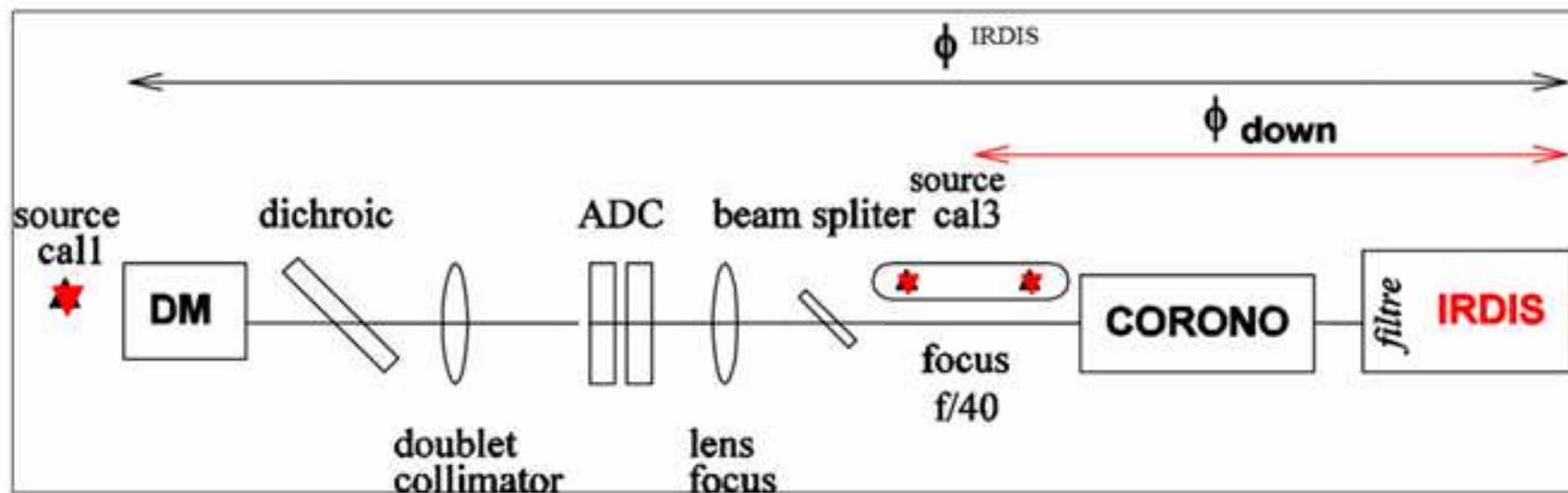
A new alternative approach : coronagraphic phase diversity (COFFEE)

- Concept
- Simulation results
- Toward an experimental validation

smart

Specificities of SPHERE NCPA calibration

- ⇒ Minimisation of the NCPA @ coronagraphic level
- ⇒ Very high accuracy : < 15 nm rms



SPHERE baseline solution

Use of classical phase diversity

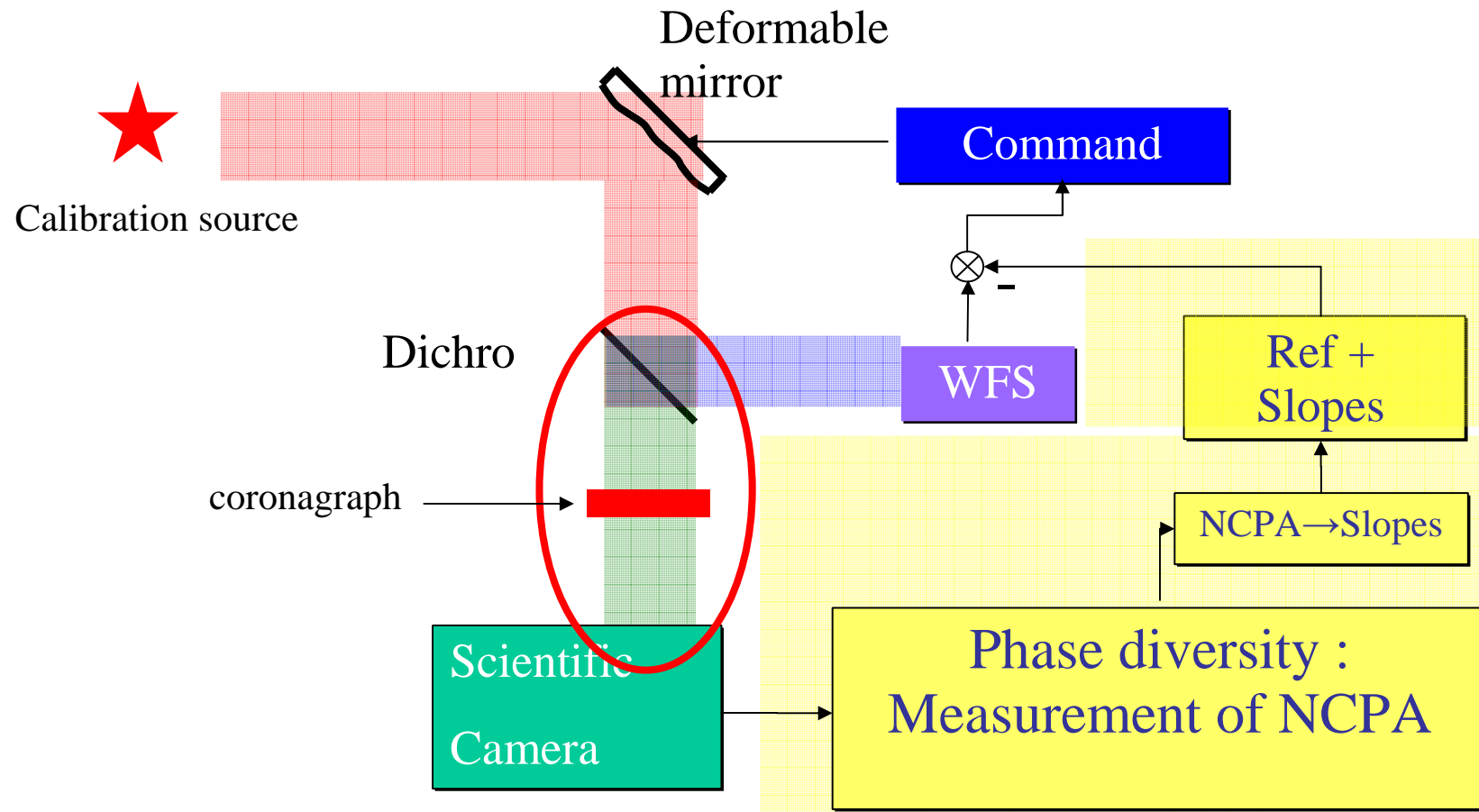
Need to remove the coronagraphic mask from the optical path

Two step measurement process:

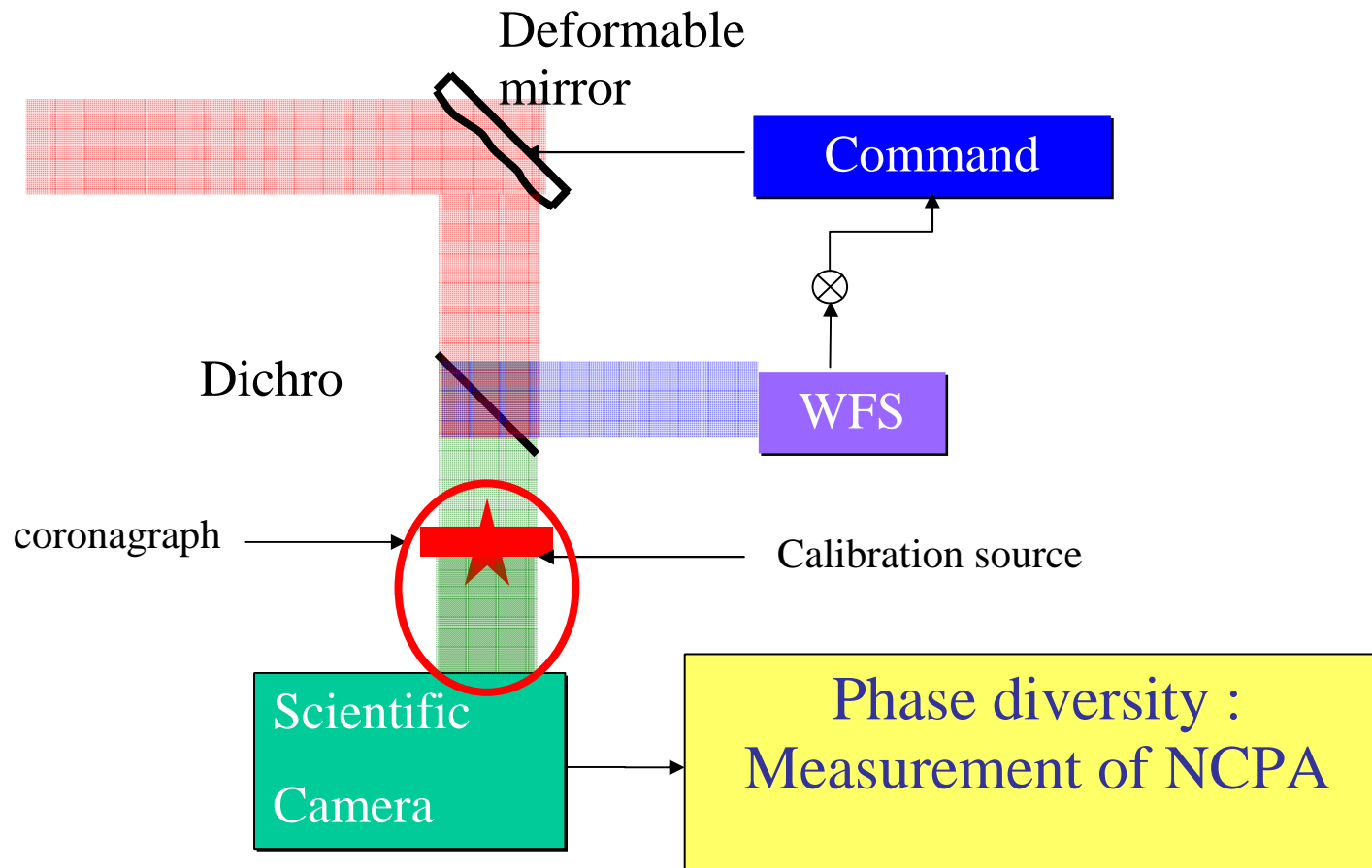
- *Measurement of φ_{IRDIS}*
(all the aberration down to IRDIS)
 - Pseudo closed loop approach
 - Diversity produced by DM

- *Measurement of φ_{down}*
(from coronagraphic focal plane down to IRDIS)
 - One shot measurement
 - Diversity provided by source motion along optical axis

Measurement of φ_{IRDIS}



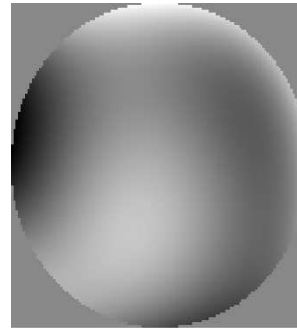
Measurement of φ_{down}



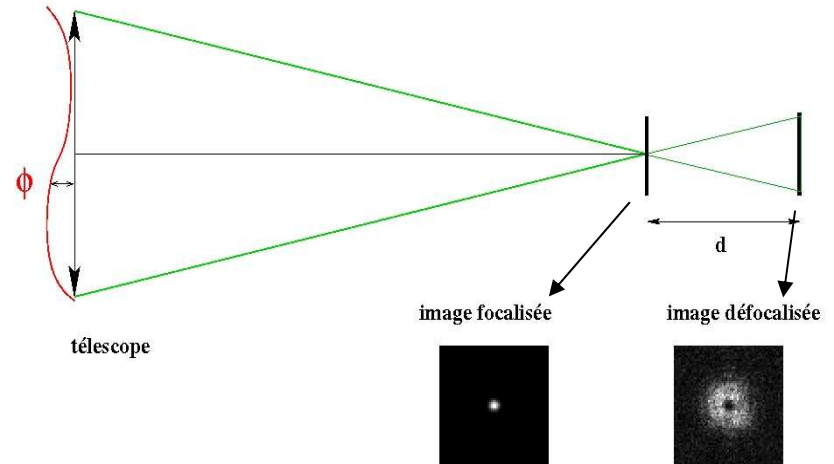
Phase diversity principle

Gonsalves, 1982

And many other since then



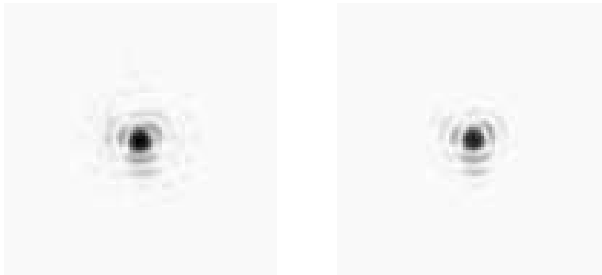
Phase dans la pupille



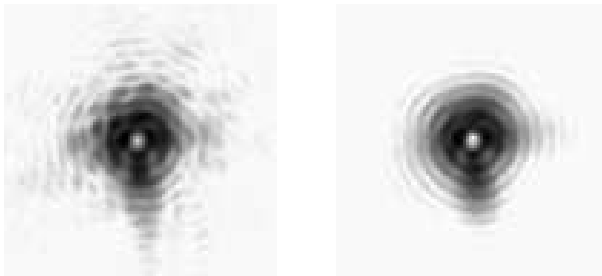
Phase diversity reconstruction

True image Estimated

Focused



Defocused



$$h = |TF^{-1} (P.e^{j\phi})|^2$$

$$h_d = |TF^{-1} (P.e^{j(\phi+\phi_d)})|^2$$

$$i_f = h_f * o + b_f$$

$$i_d = h_d * o + b_d$$

Algorithm optimisation: MAP approach

Criterion to be minimized

$$J(o, \phi) = \left\| \frac{i_f(\vec{r}) - h_f(\vec{r}) * o(\vec{r})}{\sigma_f(\vec{r})} \right\|^2 + \left\| \frac{i_d(\vec{r}) - h_d(\vec{r}) * o(\vec{r})}{\sigma_d(\vec{r})} \right\|^2 + \left(\frac{1}{2} \phi^t R_\phi^{-1} \phi \right)$$

Maximum likelihood

A priori knowledge

⇒ Regularisation term

⇒ Optical aberrations : known spectrum

- **Noise statistics :**

- **Non-uniform Gaussian law**

- ⇒ **Good approximation of photon + detector noise**

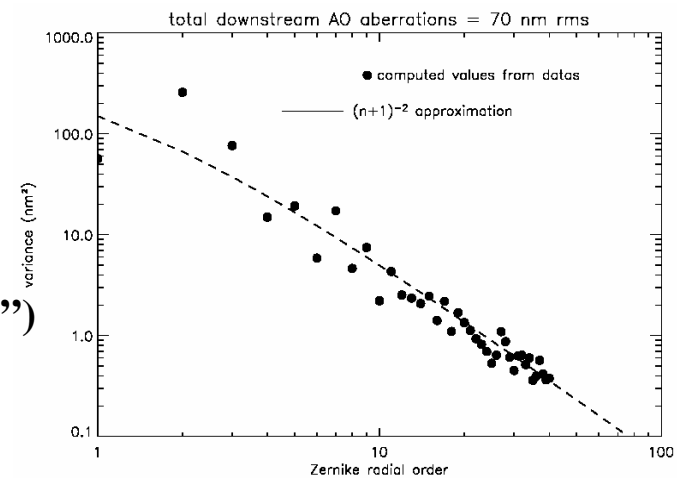
- ⇒ **Allows to deal with different exposure time between focused and defocused images**

- (↗ **SNR on defocused image**) + **pixel basis !!!!**

(the less “informative one”)

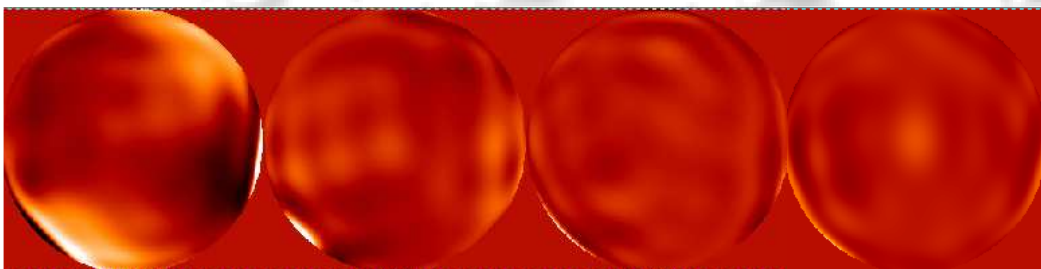
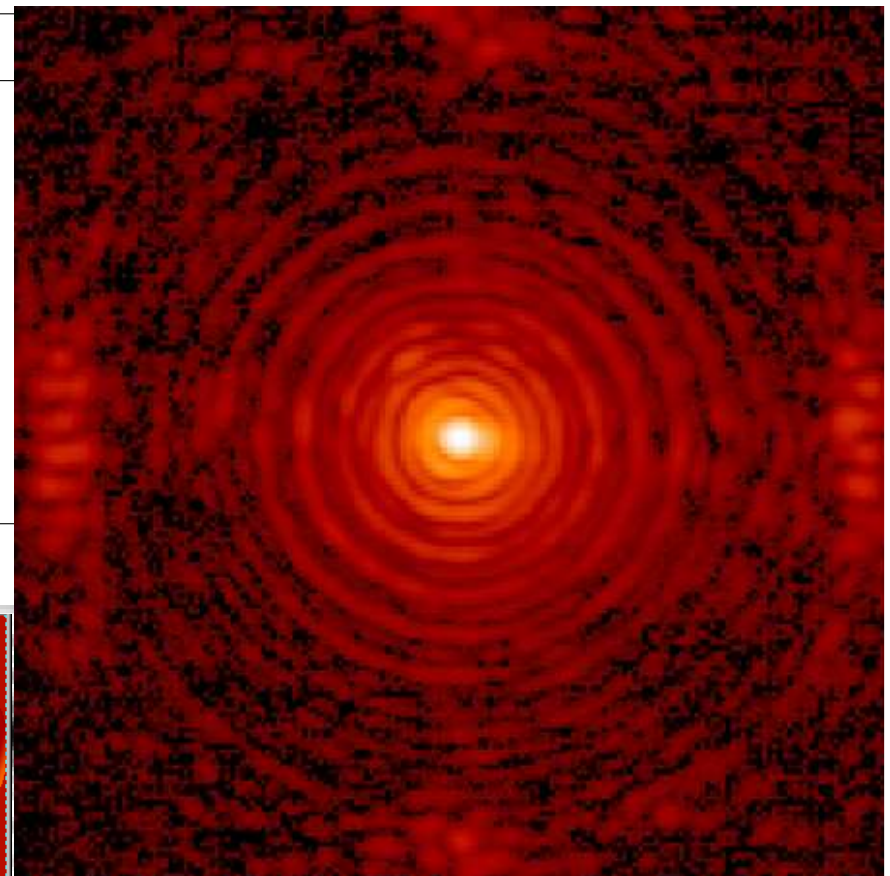
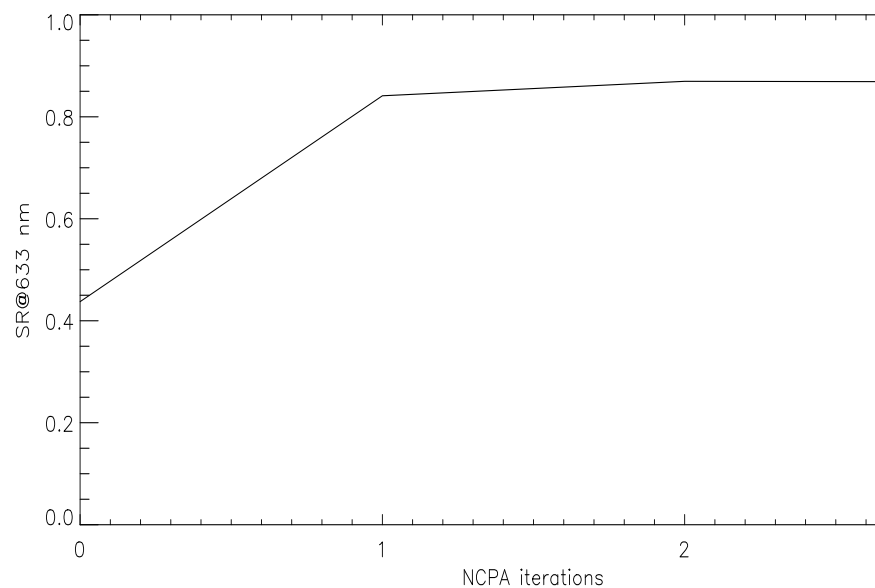
- **Estimation of object map**

⇒ Deal with Ghosts, Slightly extended object / vibrations and residual turbulence



Experimental validation of NCPA compensation on SAXO

Application of phase diversity and pseudo-closed loop scheme for NCPA correction on SAXO



An alternative approach the coronagraphic phase diversity

Modification of the "classical phase diversity" direct model

$o^*h \rightarrow Fh_c$ where F = flux and h_c = coronagraphic PSF

$$\begin{cases} h = \left| TF^{-1}(P e^{i(\phi_{total})}) \right|^2 \\ h_c = \left| TF^{-1}(P e^{i(\phi_{upstream} + \phi_{downstream})}) - \eta_0 TF^{-1}(P e^{i\phi_{downstream}}) \right|^2 \end{cases}$$

Modification of the known phase to produce diversity

Defocus (a few rad) \rightarrow sum of defocus and astig (0.8 rad each)

$$J = \left| \frac{i_c^{foc} - Fh_c^{foc}}{\sigma^{foc}} \right|^2 + \left| \frac{i_c^{div} - Fh_c^{div}}{\sigma^{div}} \right|^2 = J_{foc} + J_{diversity} \longrightarrow \text{To be minimized}$$

To be minimized w.r.t. $\phi_{upstream}$ and $\phi_{downstream}$

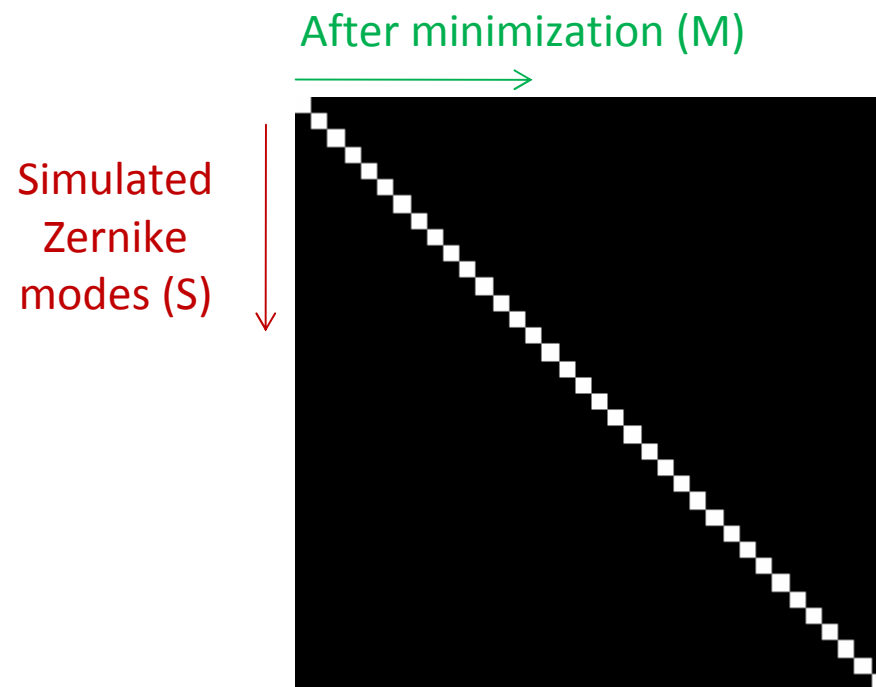
And it has a name : **COFFEE** COronagraphic Focal-plane wave-Front Estimation for Exoplanet detection

Case of the perfect coronagraph (I)

Interaction matrix

❖ Simulation :

- $WFE_{\text{upstream}} = 30 \text{ nm}$ (0,34 rad), $WFE_{\text{downstream}} = 0 \text{ nm}$ ($\lambda = 550 \text{ nm}$)
- 36 Zernike modes upstream and downstream
- Simulation : perfect coronagraph ; minimization : perfect coronagraph

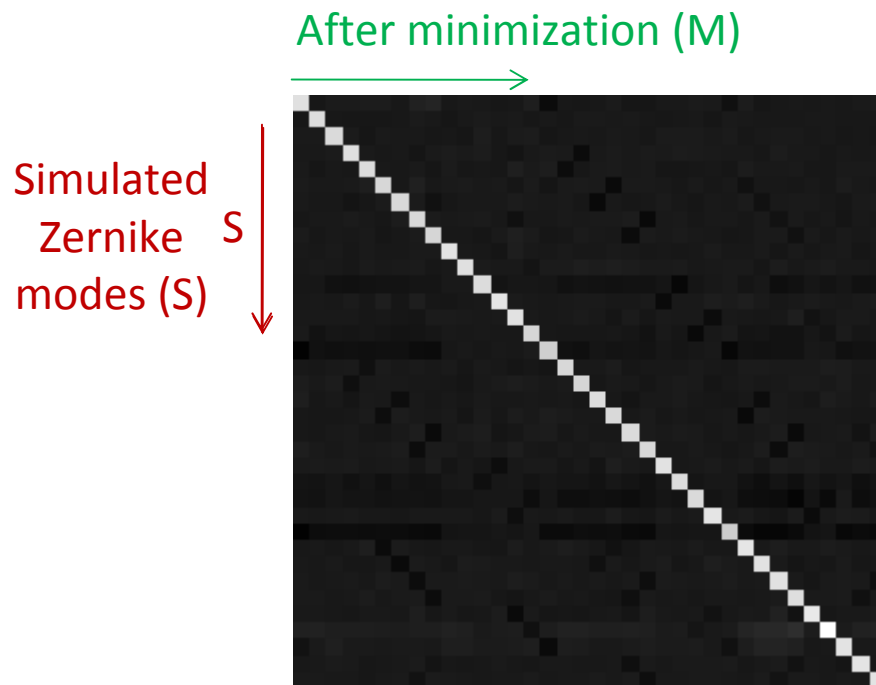


Case of the perfect coronagraph (II)

Interaction matrix with noise

❖ Simulation :

- $WFE_{\text{upstream}} = 30 \text{ nm}$, $WFE_{\text{downstream}} = 0 \text{ nm}$ ($\lambda = 550 \text{ nm}$)
- 36 Zernike modes upstream and downstream
- Simulation : perfect coronagraph ; minimization : perfect coronagraph
- Noise : shot noise, electronic noise c



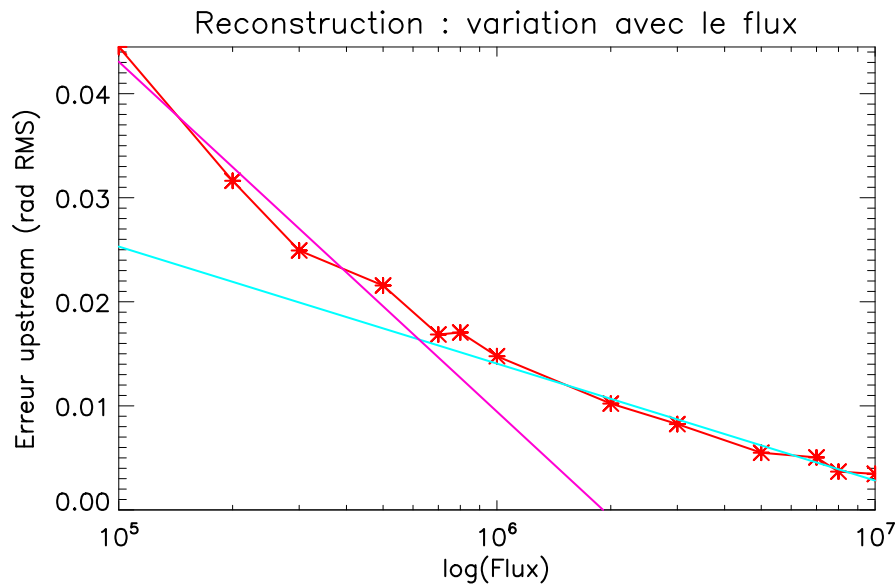
$$\mathcal{E} = \sqrt{\sum_i |a_i^{rec} - a_i^{sim}|}$$

Case of the perfect coronagraph (IV)

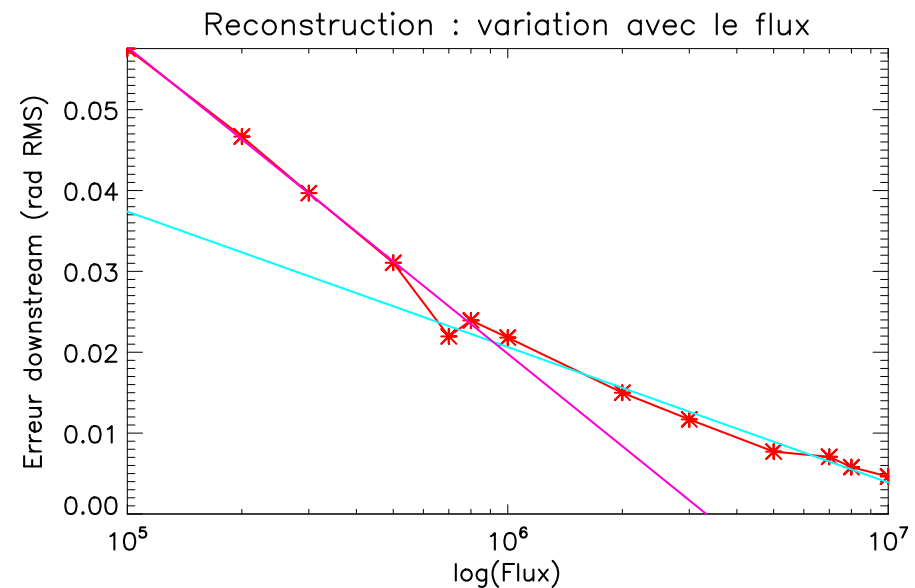
Error sensitivity : flux variations

❖ Simulation :

- $WFE_{\text{upstream}} = 30 \text{ nm}$, $WFE_{\text{downstream}} = 30 \text{ nm}$ ($\lambda = 550 \text{ nm}$)
- 36 Zernike modes upstream and downstream
- Simulation : perfect coronagraph ; minimization : perfect coronagraph
- Noise : shot noise, electronic noise



Upstream



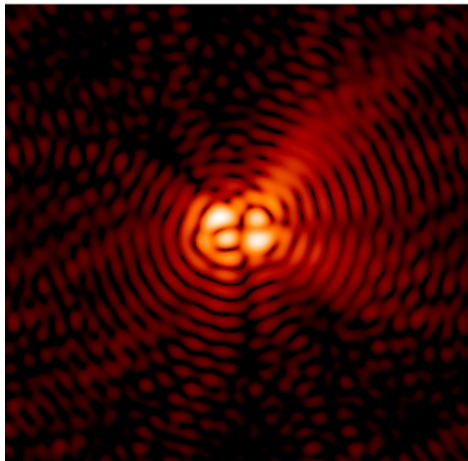
Downstream

From perfect to real coronagraphs (I)

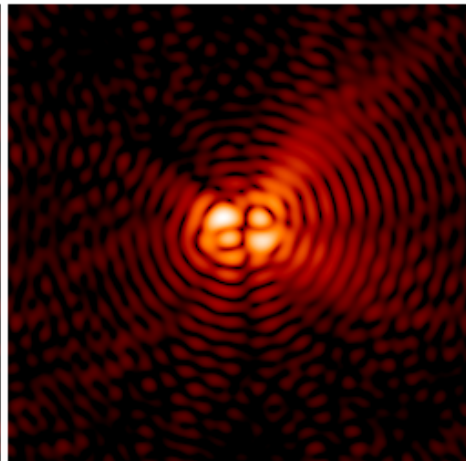
⇒ Goal : find the closest real coronagraph to the perfect model (Application of the previous model to realistic case)

⇒ Simulation :

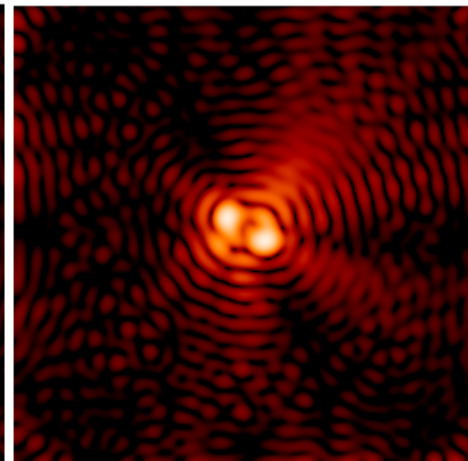
- $WFE_{\text{upstream}} = 30 \text{ nm}$, $WFE_{\text{downstream}} = 30 \text{ nm}$ ($\lambda = 550 \text{ nm}$)
- 15 Zernike modes upstream and downstream
- Phases upstream and downstream randomly generated



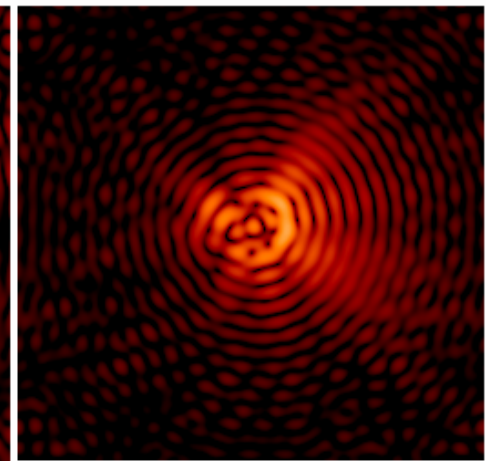
Perfect
coronagraph (PC)
= MODEL



RRPM



4QPM



Lyot
coronagraph
(Lyot stop = 0.8)

From perfect to real coronagraphs – case of the Lyot coronagraph

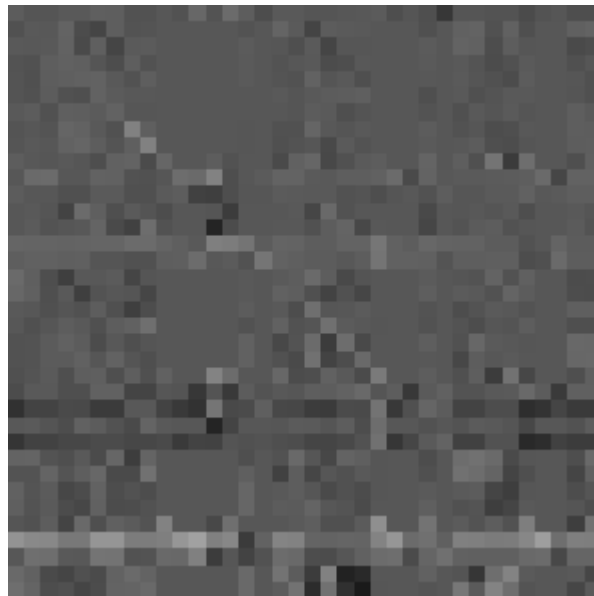
Impact on interaction matrix (no noise)

❖ Simulation :

- $WFE_{\text{upstream}} = 30 \text{ nm}$ (0,34 rad), $WFE_{\text{downstream}} = 0 \text{ nm}$ ($\lambda = 550 \text{ nm}$)
- 36 Zernike modes upstream and downstream
- Simulation : Lyot coronagraph ; minimization : perfect coronagraph
- $4 \lambda/D$ -- Lyot Stop = 0.8

After minimization (M)

Simulated
Zernike modes
(S)



From perfect to real coronagraphs – case of the Lyot coronagraph

Impact on interaction matrix (no noise)

❖ Simulation :

- $WFE_{\text{upstream}} = 30 \text{ nm}$ (0,34 rad), $WFE_{\text{downstream}} = 0 \text{ nm}$ ($\lambda = 550 \text{ nm}$)
- 36 Zernike modes upstream and downstream
- Simulation : Lyot coronagraph ; minimization : perfect coronagraph
- $4 \lambda/D$ -- Lyot Stop = 0.8



From perfect to real coronagraphs – case of the 4QPM

Impact on interaction matrix (no noise)

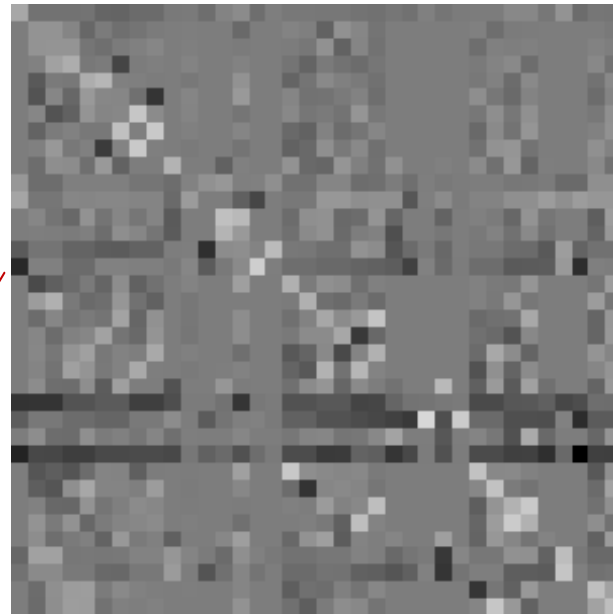
❖ Simulation :

- $WFE_{\text{upstream}} = 30 \text{ nm}$ (0,34 rad), $WFE_{\text{downstream}} = 0 \text{ nm}$ ($\lambda = 550 \text{ nm}$)
- 36 Zernike modes upstream and downstream
- Simulation : 4QPM coronagraph ; minimization : perfect coronagraph

After minimization (M)



Simulated
Zernike modes
(S)



From perfect to real coronagraphs – case of the 4QPM

Impact on interaction matrix (no noise)

❖ Simulation :

- $WFE_{\text{upstream}} = 30 \text{ nm}$ (0,34 rad), $WFE_{\text{downstream}} = 0 \text{ nm}$ ($\lambda = 550 \text{ nm}$)
- 36 Zernike modes upstream and downstream
- Simulation : 4QPM coronagraph ; minimization : perfect coronagraph



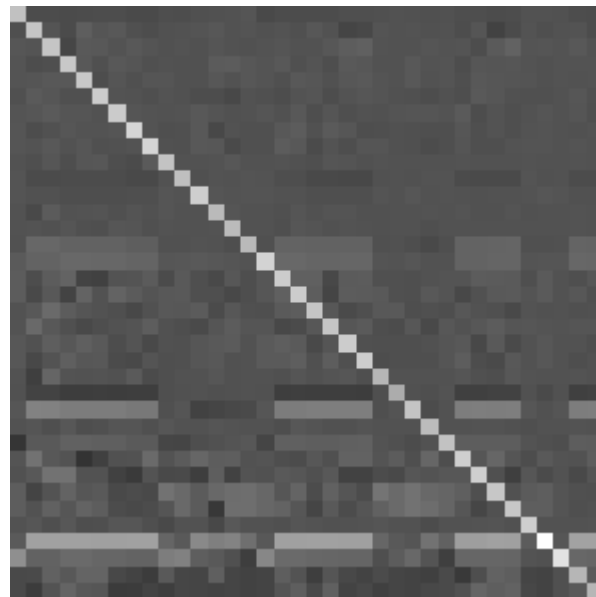
From perfect to real coronagraphs – RRPM

Impact on interaction matrix (no noise)

❖ Simulation :

- $WFE_{\text{upstream}} = 30 \text{ nm}$ (0,34 rad), $WFE_{\text{downstream}} = 0 \text{ nm}$ ($\lambda = 550 \text{ nm}$)
- 36 Zernike modes upstream and downstream
- Simulation : RRPM coronagraph ; minimization : perfect coronagraph
- 1.06 I/D – Lyot stop = 1

After minimization (M)



Simulated
Zernike modes
(S)

From perfect to real coronagraphs – RRPM

Impact on interaction matrix (no noise)

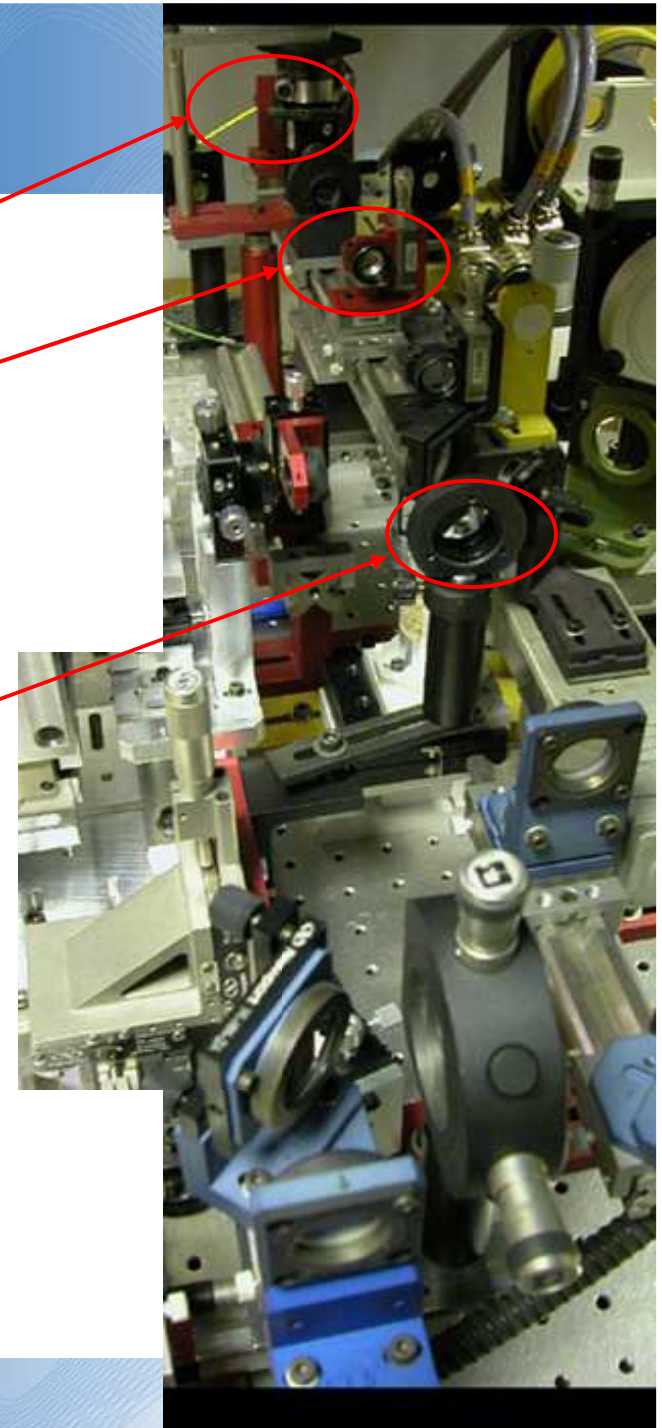
❖ Simulation :

- $WFE_{\text{upstream}} = 30 \text{ nm}$ (0,34 rad), $WFE_{\text{downstream}} = 0 \text{ nm}$ ($\lambda = 550 \text{ nm}$)
- 36 Zernike modes upstream and downstream
- Simulation : RRPM coronagraph ; minimization : perfect coronagraph
- 1.06 I/D – Lyot stop = 1

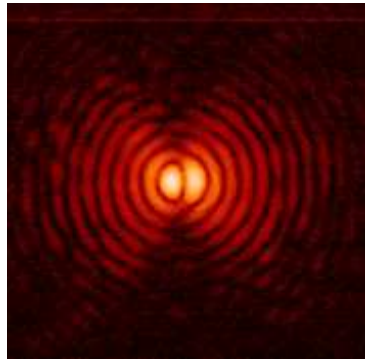


Experimental validation in progress ...

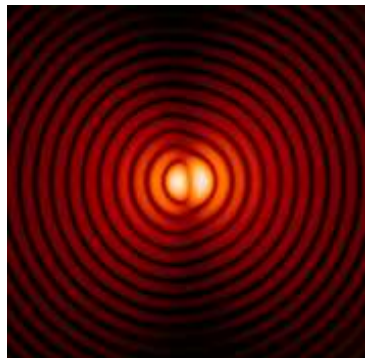
- ❖ « Non-adapted » RRPM, originally designed:
 - ❖ for $\lambda = 677\text{nm}$
 - ❖ for a FRatio of 100
 - ❖ with pupil apodization
- ❖ We used:
 - ❖ $\lambda = 675\text{nm}$
 - ❖ FRatio of 90
 - ❖ without apodization
- ❖ Tilt introduction : coronagraphic mask shift
→ corresponds to a beam shift on the coronagraphic mask



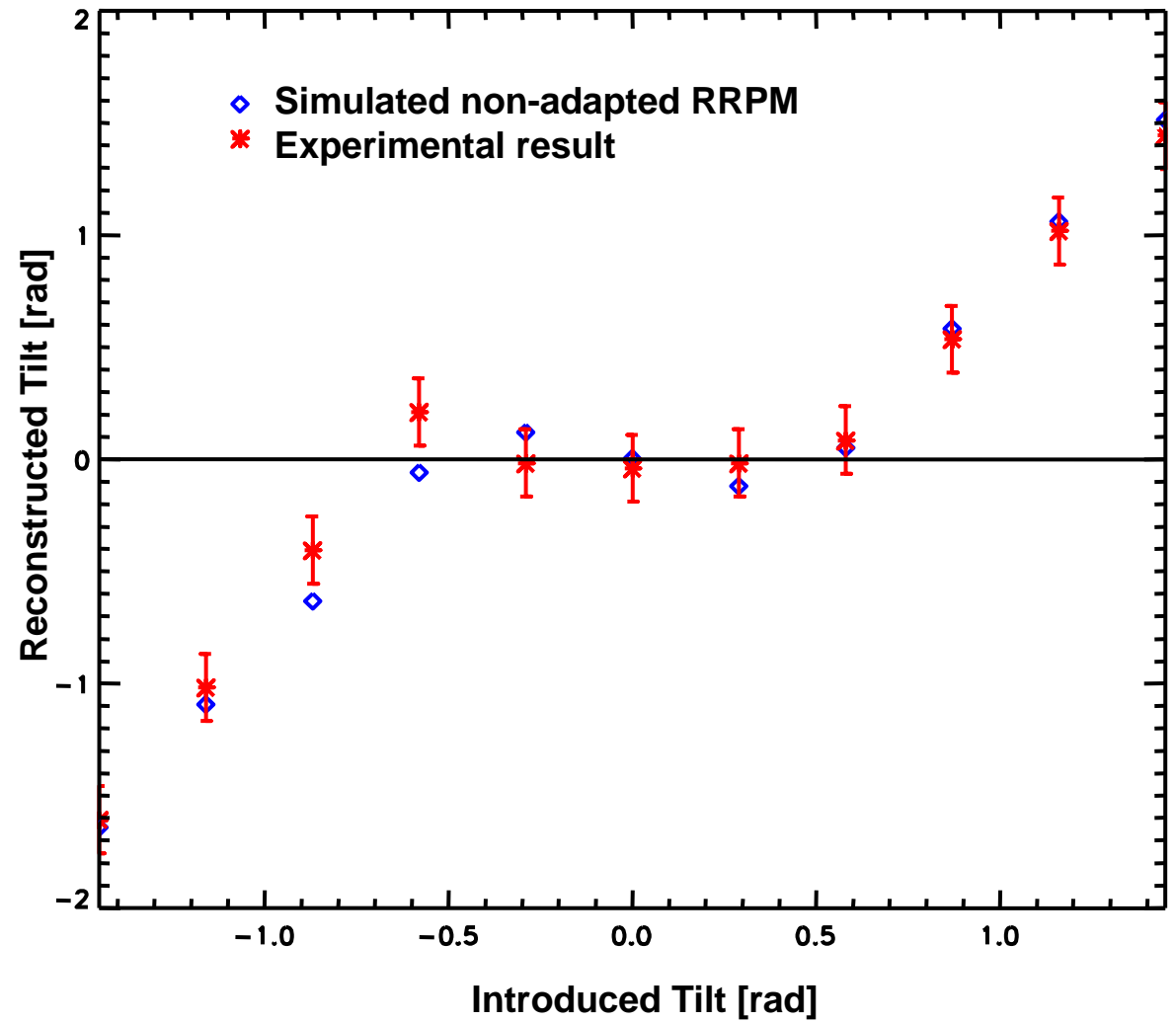
Very first result : reconstruction of a tilt ramp



Exp image



Reconstructed



Conclusions

NCPA pre-compensation for SPHERE : very challenging process

- Very tight performance
- Minimization on coronagraphic mask and not scientific detector
- ⇒ Complex procedure
- ⇒ Fully studied and optimized in simulation
- ⇒ First experimental results => residual = 16 nm rms (without any optimisation)

Full validation of COFFEE by simulation

- Based on « perfect coronagraph » model
- Estimation of both $\phi_{upstream}$ and $\phi_{downstream}$ aberrations on 2 images
- Proposition of a mixed phase diversity defoc + astig
- Classical behaviour wrt noise
- Tested robustness to realistic coronagraph: RRPM

Very first experiments with COFFEE on « non-adapted » RR mask

- seem to be coherent with simulation

Perspectives

Full experimental validation at ONERA with LAM support

- Tip-Tilt and Low orders estimation
- High orders estimation

Extension of coronagraphic imaging model to other coronagraph (4Q, Lyot)

Extension to AO-corrected long exposure images

Extrapolation of performance on SPHERE system