

# Point Spread Function Reconstruction for Laser Guide Star Tomography Adaptive Optics

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# Presentation Outline

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- What is Adaptive Optics (AO) Point Spread Function Reconstruction (PSFR) ? Why is it important ?
- Basic idea developed by Véran in 1997
- Extensions to tomography AO
- Work done to date
- Work in progress

## What is AO PSFR ?

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- Estimation of the science long-exposure OTF (Fourier transformed PSF) from AO system RTC telemetry
    - Problem reduced to estimation of residual science wavefront covar. matrix from RTC telemetry data
    - RTC telemetry data: error covar. matrix, traditionally in WFS space, but could equally be in DM actuator space
  - Required in order to perform image de-convolution
  - Essential to retrieve high angular resolution information in any AO astronomical science program
    - Photometry and astrometry
    - Precision orbits estimation at the Galactic Center, etc.

## Basic idea developed by Véran JOSA A 1997

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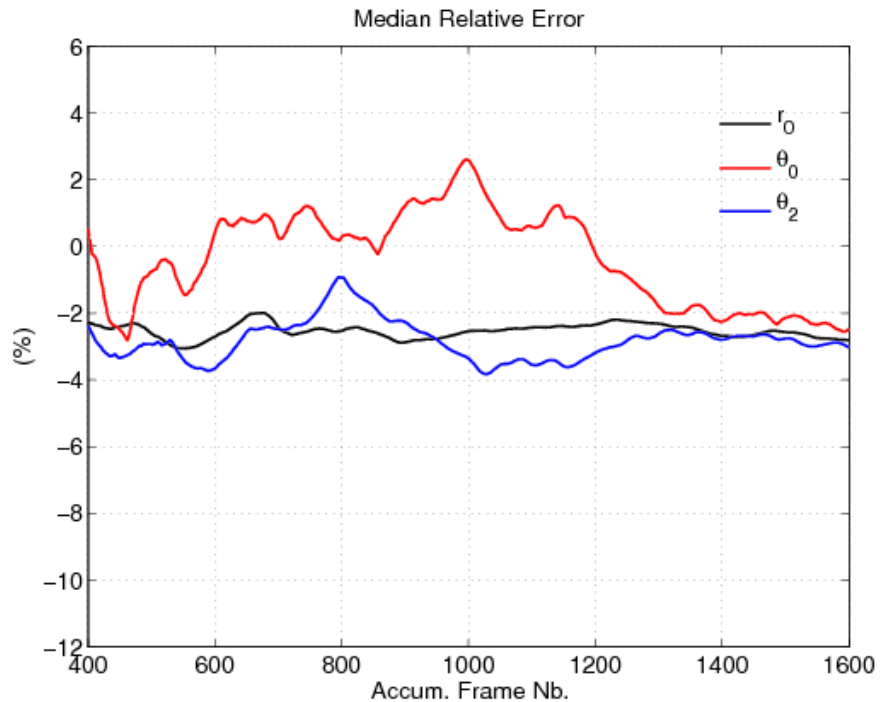
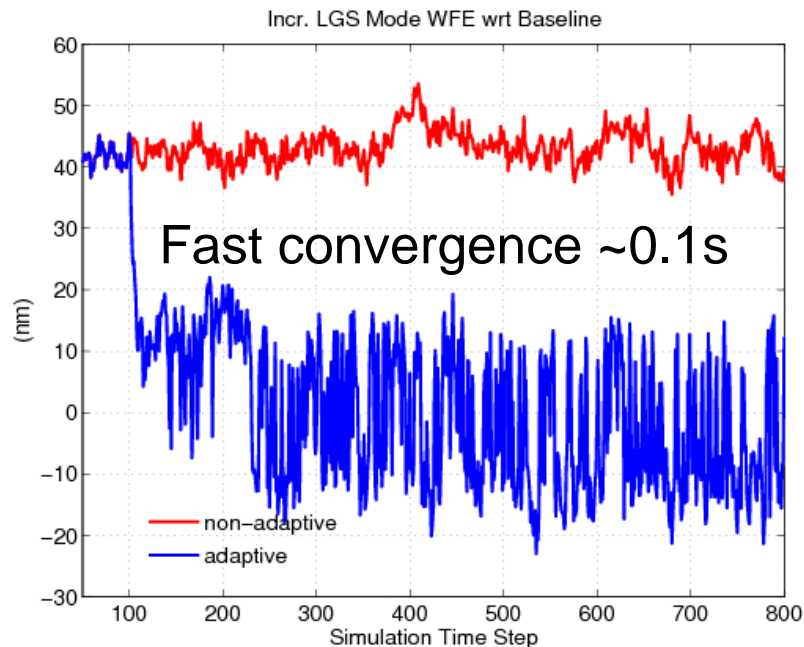
- RTC WFS measurement covariance matrix corrupted by noise and aliasing that need to be “taken out”
- Residual WFE left over and seen by WFS is servo-lag, obtained by mapping de-noised, de-aliased measurement covar. matrix onto DM actuator space with least-squares reconstructor
- AO telemetry does not see everything:
  - Anisoplanatism WFE (depends on Cn2 profile): angular (Fusco 2000, Britton 2006), focal (Flicker 2008) for LGS
  - DM fitting WFE
  - Non-common path aberrations (NCPA) (including instrument distortion errors)

## Extension to Laser Tomography AO

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- What RTC telemetry data to use ?
    - WFS: mapping de-noised, de-aliased multi-WFS measurement covar. matrix onto DM actuator space with tomographic reconstructor off-line is impractical
    - **RTC does tomography for you, so use it !**
  - Bonuses:
    - Uses RTC built-in SLODAR
    - Uses covar. matrix of summed LGS loop and NGS loop actuator error signals to preserve cross-coupling
  - Off-line steps (require Cn2 profile) :
    - De-noise, de-alias with separate LGS mode and NGS mode covar. matrices
    - Compute unseen DM (generalized) fitting covar. matrices, either analytically in FD or by simulation

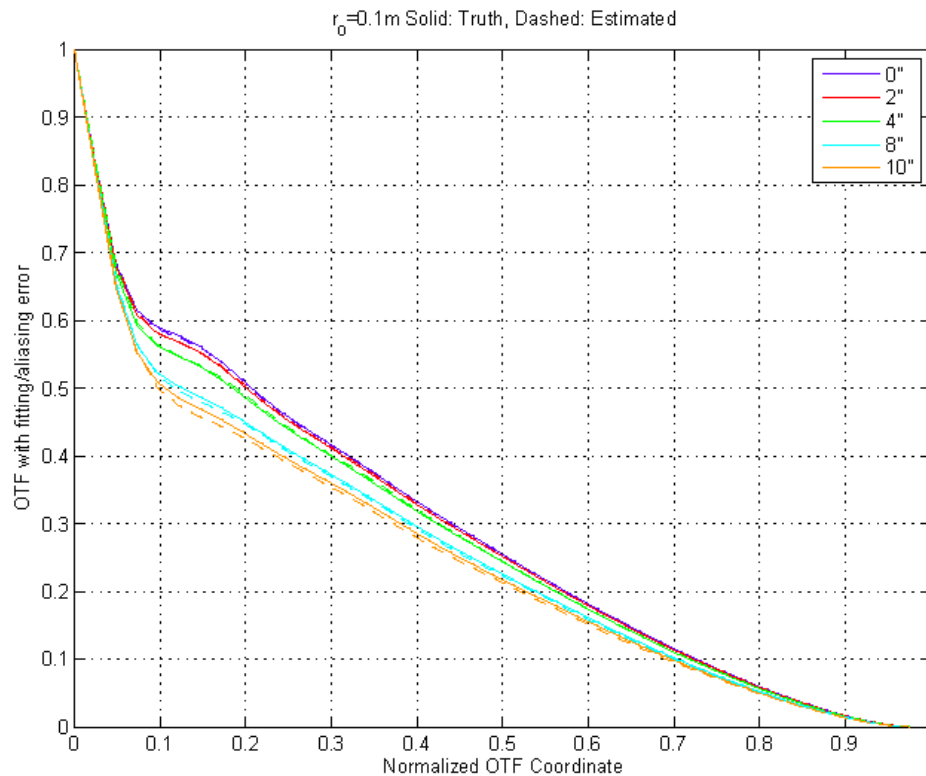
# NFIRAOS built-in LGS SLODAR (Gilles, JOSA A 2010)

- 12-layer profile reconstructed in RTC from a pair of LGS WFS (1' apart) pseudo open loop cross-covar.
- Insensitive to LGS tip/tilt/focus
- Adaptively binned in RTC to update 6-layer LGS tomography algorithm

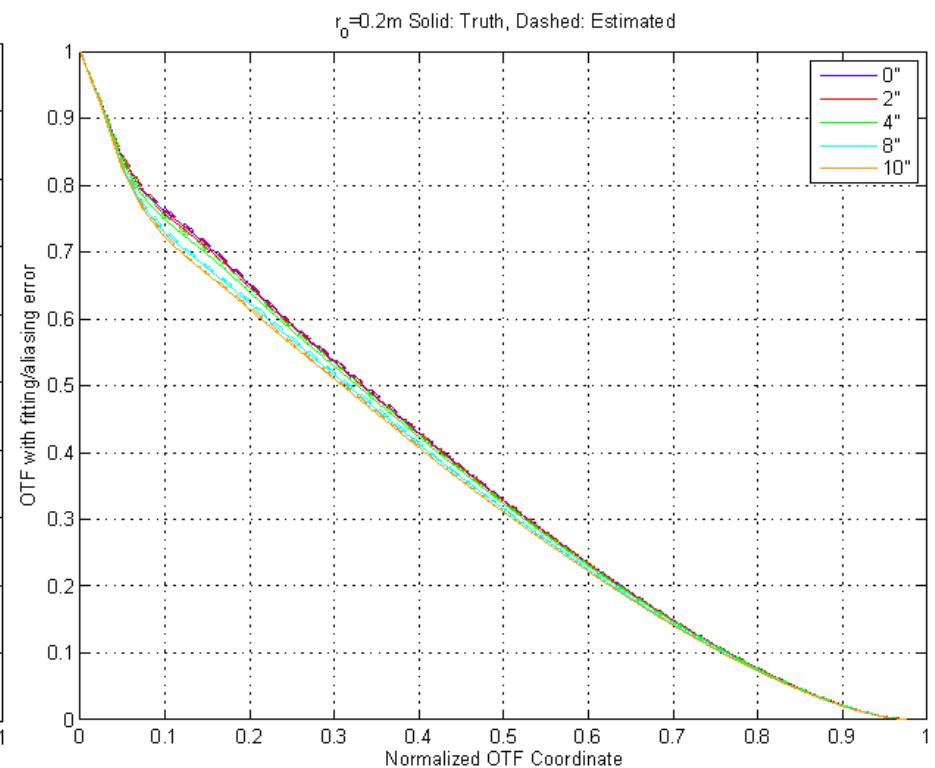


## Work done to date on tomography approach

- Successfully validated on- and off-axis for classical NGS AO and NGS MCAO (6-layer tomography performed using NFIRAOS RTC CG algorithm)



(a)  $r_0=0.1\text{m}$ . On axis Strehl error is -0.47%.



(d)  $r_0=0.2\text{m}$ . On axis Strehl error is -1.3%

## Less natural extension

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- RTC telemetry data: single LGS WFS measurement covar. matrix, and NGS mode error covar. matrix
  - Off-line steps (require Cn2 profile estimate):
    - De-noise, de-alias LGS WFS covar. matrix
    - Map onto wavefront space by appropriate reconstructor
    - Extrapolate to science (LGS mode tomography error)
    - Compute unseen DM (generalized) fitting cov. matrix
    - De-noise, de-alias NGS mode error covar. matrix and sum to LGS mode covar. matrix

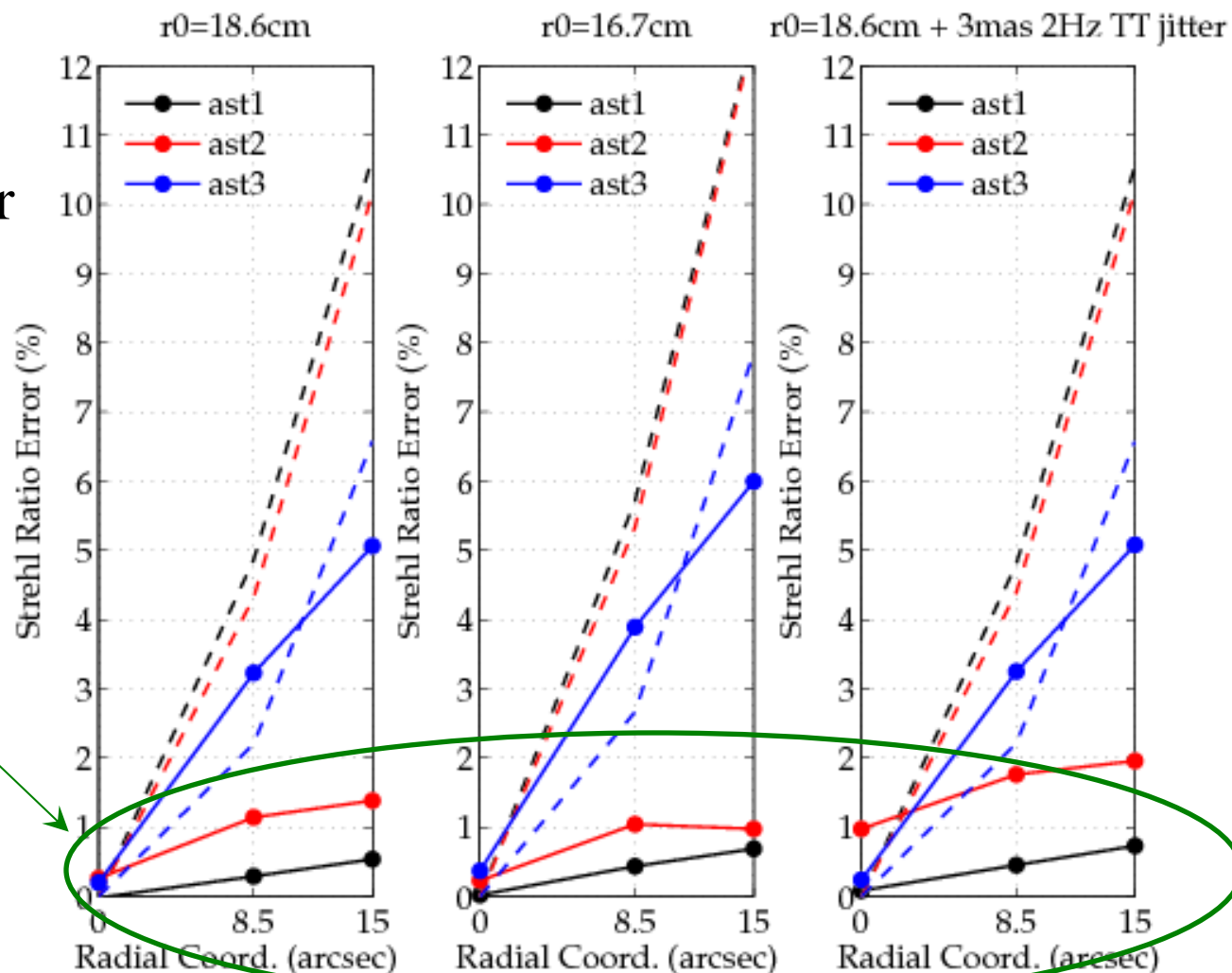


# Preliminary Assessment of LGS/NGS-mode decoupling

- Dashed curves are science SR variations. Indicate diff. photometry error when using on-axis PSF off-axis

- PSF variability reduced ~10X

- NFIRAOS 2% Diff. Photometry Req. met provided all PSFR errors fit within a ~1% SR error budget !



## LGS-to-Science Extrapolation

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- ◆ Key: work with Structure Function (SF) matrix.  
Trivially computed with linear operations on the covariance matrix.
- ◆ Compute a LGS-to-science “SF filter”, expressed as a SF ratio, computed by simulation (fed by average Cn2 profile)
  - Proven to be robust against seeing model error, since both LGS and LGS mode science SF scale as the negative 5/3th power of the Fried parameter
- ◆ Note: alternative approach to SF is to use a log OTF (aperture-averaged SF)
  - Proven to be equally insensitive to seeing model error

# NGS-mode error covariance matrix de-noising and de-aliasing

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- ◆ Common step to both approaches
- ◆ De-noising is challenging for dim NGS asterisms
- ◆ De-aliasing is challenging. Successful method hasn't been found yet. Ignoring aliasing penalizes SR estimate by ~4-8% error for median sky coverage NGS asterisms for NFIRAOS, blowing up photometry error budget...

## Work in progress

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- ◆ NGS mode aliasing covar. matrix or ways to reduce aliasing
- ◆ End-to-end performance and robustness assessment of both approaches for NFIRAOS (LGS MCAO)

## Acknowledgements

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